Big Ideas	Details L	Jnit: Mathematics			
honors & AP®	Solving Equations Symbolically				
	 Unit: Mathematics NGSS Standards/MA Curriculum Frameworks (2016): SP5 AP® Physics 1 Learning Objectives/Essential Knowledge (2024): SF Mastery Objective(s): (Students will be able to) Rearrange algebraic expressions to solve for any variable in the Success Criteria: Rearrangements are algebraically correct. Language Objectives: Describe how the rules of algebra are applied to expressions variables. Tier 2 Vocabulary: equation, variable 	P2.A he expression.			
	Notes: In solving physics problems, we are more often interested in the rebetween the quantities in the problem than we are in the numerical For example, suppose we are given a problem in which a person wi 65 kg accelerates on a bicycle from rest $(0 \frac{m}{s})$ to a velocity of $10 \frac{m}{s}$ of 12 s and we wanted to know the force that was applied. We could calculate acceleration as follows: $v - v_o = at$ 10 - 0 = a(12) $a = \frac{10}{12} = 0.8\overline{3} \frac{m}{s^2}$ Then we could use Newton's second law: F = ma $F = (65)(0.8\overline{3}) = 54.2 \text{ N}$ We have succeeded in answering the question. However, the quess answer are of no consequence. Obtaining the correct answer show manipulate two related equations and come out with the correct n	tion and the vs that we can			

Use this space for summary and/or additional notes:

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honors & AP®	However, if instead we decided that we wanted to come up wit force in terms of the quantities given (mass, initial and final velo would need to rearrange the relevant equations to give an expr terms of those quantities.	ocities and time), we
	Just like algebra with numbers, rearranging an equation to solve simply "undoing PEMDAS:"	e for a variable is
	 "Undo" addition and subtraction by doing the inverse (of If a variable is added, subtract it from both sides; if the variable add it to both sides. 	
	a+c=b	
	-c = -c	
	a = b - c	
	2. "Undo" multiplication and division by doing the inverse of variable is multiplied, divide both sides by it; if the variable denominator, multiply both sides by it. Note: whenever the denominator that are on the same side of the equation you are solving for, always multiply both sides by it to cle	ble is in the you have variables in on as the variable
	$\frac{n}{r} = s$ $\frac{xy}{y} = \frac{z}{y}$ $x = \frac{z}{y}$ $\frac{n}{s} = s \cdot r$ $n = sr$ $\frac{n}{s} = s$ $\frac{n}{s} = r$	
	 S 3. "Undo" exponents by the inverse operation, which is tak root of both sides. (Most often, the exponent will be 2, where the square root.) Similarly, you can "undo" roots by raising appropriate power. 	which means take
	$t^2 = 4ab$	
	$\sqrt{t^2} = \sqrt{4ab}$	
	$t = \sqrt{4} \cdot \sqrt{ab} = 2\sqrt{ab}$	
	 When you are left with only parentheses and nothing ou can drop the parentheses, and then repeat steps 1–3 abo nothing left but the variable of interest. 	-

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honors & AP®	Returning to the previous problem:	
	We know that $F = ma$. We are given m , but not a , which mean a with an expression that includes only the quantities given.	s we need to replace
	First, we find an expression that contains <i>a</i> :	
	$v - v_o = at$	
	We recognize that $v_0 = 0$, and we use algebra to rearrange the respective recognize that v_0 = 0, and everything else is on the other side	
	v = at	
	_	
	$\underline{a} = \frac{v}{t}$	
	Finally, we replace <i>a</i> in the first equation with $\frac{v}{t}$ from the second	nd:
	F = ma	
	$F = (m)(\frac{v}{t})$	
	$F = \frac{mv}{t}$	
	If the only thing we want to know is the value of <i>F</i> in one specific substitute numbers at this point. However, we can also see from that increasing the mass or velocity will increase the numerator the value of the fraction, which means the force would increase that increasing the time would increase the denominator, which value of the fraction, which means the force would decrease.	m our final equation , which will increase . We can also see
	Solving the problem symbolically gives a relationship that holds of this type in the natural world, instead of merely giving a num single pointless question. This is why the College Board and ma insist on symbolic solutions to equations.	ber that answers a
I	۱ <u>ــــــــــــــــــــــــــــــــــــ</u>	

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	1.	(S) Given $a = 2bc$ and $e = c^2 d$, write an expression for and d .	⁻ e in terms of a, b,	
	2.	(M) Given $w = \frac{3}{2}xy^2$ and $z = \frac{q}{y}$:		
		a. (M) Write an expression for <i>z</i> in terms of <i>q</i> , <i>w</i> ,	and <i>x</i> .	
		 (M) If you wanted to maximize the value of the question #2 above, what adjustments could yo of q, w, and x? 		
		c. (M) Changing which of the variables q, w, or x largest change in the value of z?	would give the	

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