Big Ideas	Details Unit: Mathematics
	Vectors
	Unit: Mathematics
	NGSS Standards/MA Curriculum Frameworks (2016): SP5
	AP [®] Physics 1 Learning Objectives/Essential Knowledge (2024): 1.1.A.1, 1.1.A.2, 1.1.A.3, 1.1.A.3.i, 1.1.A.3.ii, 1.1.B.1, 1.5.A, 1.5.A.1, 1.5.A.2, 1.5.A.3
	Mastery Objective(s): (Students will be able to)
	 Identify the magnitude and direction of a vector.
	 Combine vectors graphically and calculate the magnitude and direction. Success Criteria:
	 Magnitude is calculated correctly (Pythagorean theorem).
	 Direction is correct: angle (using trigonometry) or direction (<i>e.g.,</i> "south", "to the right", "in the negative direction", <i>etc.</i>)
	Language Objectives:
	 Explain what a vector is and what its parts are.
	Tier 2 Vocabulary: magnitude, direction
	Notes:
	vector: a quantity that has a direction as well as a magnitude (value/quantity).
	<i>E.g.,</i> if you are walking $1\frac{m}{s}$ to the north, the magnitude is $1\frac{m}{s}$ and the direction is north.
	scalar: a quantity that has a value/quantity but does not have a direction. (A scalar is what you think of as a "regular" number, including its unit.)
<u>!</u>	magnitude: the part of a vector that is not the direction (<i>i.e.,</i> the value including its units). If you have a force of 25 N to the east, the magnitude of the force is 25 N.
	The mathematical operation of taking the magnitude of a vector is represented by two double vertical bars (like double absolute value bars) around the vector. For example, if \vec{F} is 25 N to the east, then $\ \vec{F}\ = 25 \text{ N}$. However, to make
	typesetting easier, it is common to use regular absolute value bars instead, <i>e.g.</i> , $\left \vec{F}\right = 25 \text{N}$.
	resultant: a vector that is the result of a mathematical operation (such as the addition of two vectors).
	Use this space for summary and/or additional notes:

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	Variables that represent vectors are traditionally typeset in b variables may also optionally have an arrow above the letters	
	J, Ē, v	
	Variables that represent scalars are traditionally typeset in <i>pl</i>	ain Italics:
	<i>V, t,</i> λ	
	Variable that represent only the magnitude of a vector (<i>e.g.,</i> direction is not relevant) are typeset as if they were scalars:	in equations where the
	For example, suppose \vec{F} is a vector representing a force (Notice that the vector includes the magnitude or amoun	
	If we needed a variable to represent only the magnitude the variable <i>F</i> .	of 25 N, we would use
	Vectors are represented graphically using arrows. The length represents the magnitude of the vector, and the direction of the direction of the vector:	
	$\xrightarrow{10}$ \leftarrow $\xrightarrow{15}$	1 7
	magnitude 10 magnitude 15 m	nagnitude 7
		direction: "up", +90°
	The negative of a vector is a vector with the same magnitude direction:	in the opposite
	$\xrightarrow{10}$ \leftarrow^{-10}	-
	Note, however, that we use positive and negative numbers to direction of a vector, but a negative value for a vector does n as a negative number in mathematics. In math, $-10 < 0 < -10$ and negative numbers represent locations on a continuous n	ot mean the same thing +10, because positive
	However, a velocity of $-10\frac{m}{s}$ means " $10\frac{m}{s}$ in the negative d	irection". This means
	that $-10\frac{m}{s} > +5\frac{m}{s}$, because the first object is moving faster	-
	<i>vs.</i> $5\frac{m}{s}$), even though the objects are moving in opposite dire	ections.
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Details

Translating Vectors

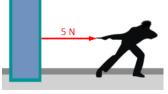
Vectors have a magnitude and direction but not a location. This means we can translate a vector (in the geometry sense, which means to move it without changing its size or orientation), and it's still the same vector quantity.

For example, consider a person pushing against a box with a force of 5 N to the right. We will define the positive direction to be to the right, which means we can call the force +5 N:

If the force is moved to the other side of the box, it's still 5 N to the right (+5 N), which means it's still the same vector:

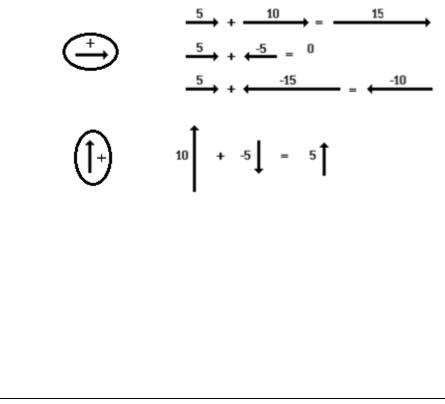


5 N

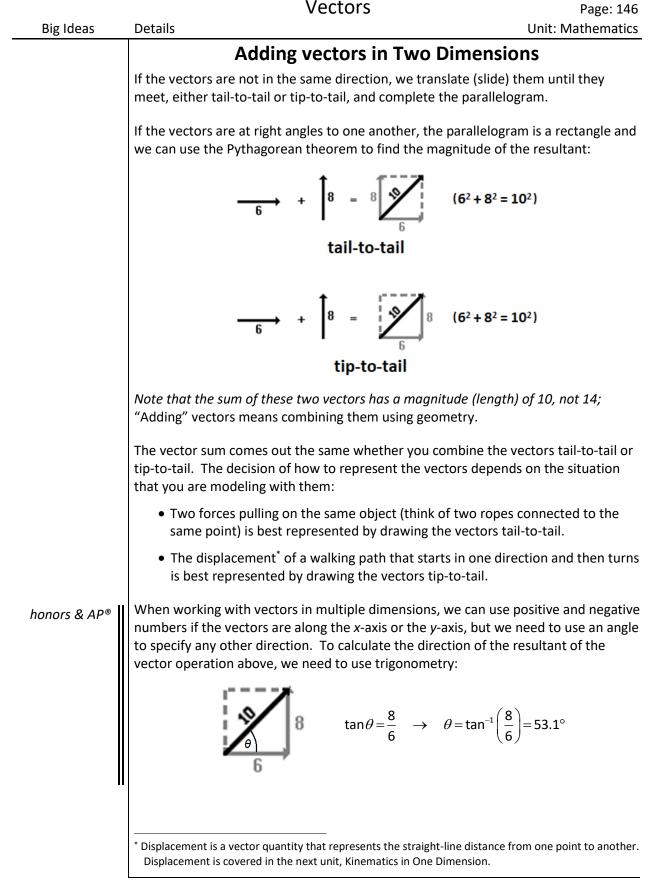


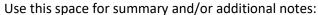
Adding Vectors in One Dimension

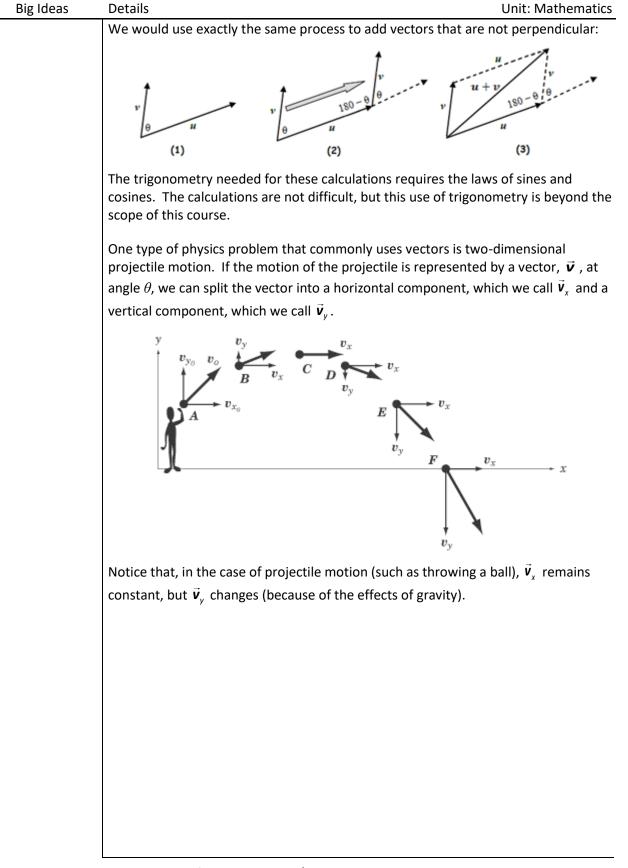
If you are combining vectors in one dimension (*e.g.*, horizontal), adding vectors is just adding positive and/or negative numbers:



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Vectors

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Because perpendicular vectors do not affect each other, we can apply equations to the two directions separately.

For example, in projectile motion (which you will learn about in detail in the Projectile Motion topic starting on page 226), we usually use the equation $\vec{d} = \vec{v}_o t + \frac{1}{2}\vec{a}t^2$, applying it separately in the *x*- and *y*-directions. This gives us two equations.

In the horizontal (x)-direction:

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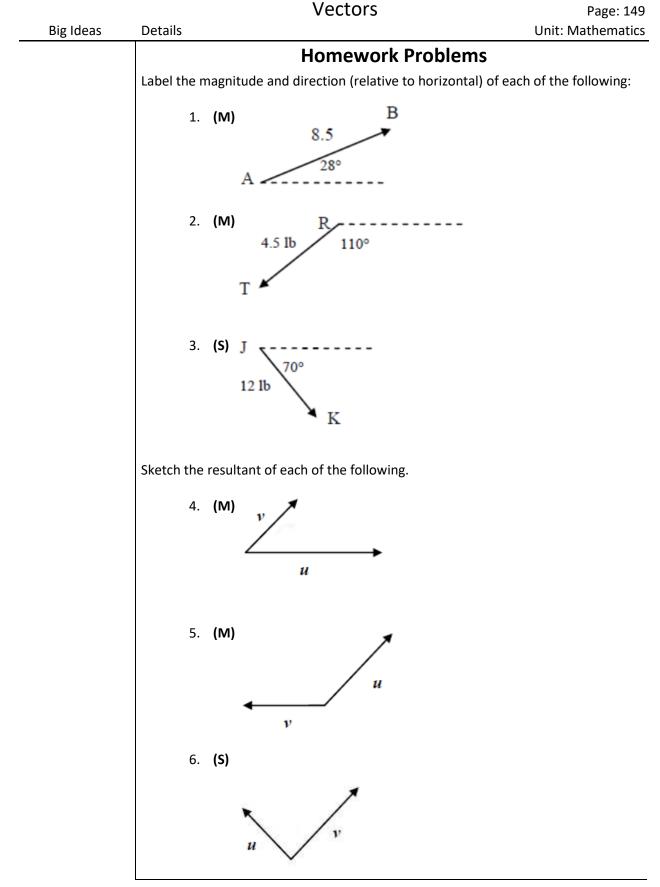
$$\vec{d}_x = \vec{v}_{o,x}t + \frac{1}{2}\vec{a}_x^{(0)}t^2$$
$$\vec{d}_x = \vec{v}_x t$$

In the vertical (y)-direction:

$$\vec{\boldsymbol{d}}_{y} = \vec{\boldsymbol{v}}_{o,y}t + \frac{1}{2}\vec{\boldsymbol{a}}_{y}t^{2}$$
$$\vec{\boldsymbol{d}}_{y} = \vec{\boldsymbol{v}}_{o,y}t + \frac{1}{2}\vec{\boldsymbol{g}}t^{2}$$

Note that each of the vector quantities (\vec{d} , \vec{v}_o and \vec{a}) has independent *x*- and *y*components. For example, $\vec{v}_{o,x}$ (the component of the initial velocity in the *x*direction) is independent of $\vec{v}_{o,y}$ (the component of the initial velocity in the *x*direction). This means we treat them as completely separate variables, and we can solve for one without affecting the other.

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g Ideas Details		Unit: Mathema
Conside	r the following vectors $\vec{A} \otimes \vec{B}$.	
	\vec{A} has a magnitude of 9 and its n is the positive horizontal direction right).	$\vec{A} - 9$ $\vec{B} - \vec{B}$
	B has a magnitude of 12 and its n is the positive vertical direction	→ ↓
	7. (M) Sketch the resultant of $\vec{A} + \vec{B}$, and de direction [*] .	etermine its magnitude an
	8. (S) Sketch the resultant of $\vec{A} - \vec{B}$ (which is determine its magnitude and direction [*] .	s the same as $ec{m{A}}+(-ec{m{B}})$, an
		the same as $ec{m{A}}+(-ec{m{B}})$, an
		s the same as $ec{m{A}}+(-ec{m{B}})$, an
		the same as $ec{A} + (-ec{B})$, an
		the same as \vec{A} + ($-\vec{B}$) , an
		s the same as $ec{m{A}}+(-ec{m{B}})$, an
		the same as \vec{A} + ($-\vec{B}$) , an

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