| Big Ideas | Details | - 0 | Inear & Rotational | | | - | | |
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| AP® | | | | | | | | |
| , (| Solving Ellear & Rotational Motion Provident | | | | | | | |
| | Unit: Kinematics (Motion) in Multiple Dimensions | | | | | | | |
| | NGSS Standards/MA Curriculum Frameworks (2016): N/A AP [®] Physics 1 Learning Objectives/Essential Knowledge (2024): 5.1.A, 5.1.A.1, | | | | | | | |
| | 5.1.A.1.i, 5.1.A.1.ii, 5.1.A.1.iii, 5.1.A.2, 5.1.A.3, 5.1.A.4, 5.1.A.4.i, 5.1.A.4.ii, 5.2.A, 5.2.A.2, 5.2.A.3 | | | | | | | |
| | Mastery Objective(s): (Students will be able to) | | | | | | | |
| | Solve problems involving any combination of linear and/or angular motion. | | | | | | | |
| | Success Criteria: | | | | | | | |
| | Correct quantities are identified and correct variables are chosen for each dimension. | | | | | | | |
| | Algebra is correct and rounding to appropriate number of significant figures is reasonable. | | | | | | | |
| | Langua | ge Obje | ectives: | | | | | |
| | • 0 | orrect | y identify quantities with r | espect | to type of c | uantity and direction in | | |
| | | | oblems. | | | | | |
| | | • | variables correctly in word | problei | ms. | | | |
| | Tier 2 v | ocabu | lary: N/A | | | | | |
| | Notes: | | | | | | | |
| | The following is a summary of the variables used for motion problems. Note the | | | | | | | |
| | | - | • | | | • | | |
| | | - | is a summary of the variab ce between the linear and | | | • | | |
| | | - | • | | r quantities | Angular | | |
| | corresp Var. | onden Unit | ce between the linear and Linear Description | angula Var. | r quantities Unit | Angular Description | | |
| | corresp Var. | ondeno Unit m | ce between the linear and Linear Description position | angula Var. θ | r quantities Unit rad (—) | Angular Description angle; angular position | | |
| | corresp Var. x d,∆x | ondeno Unit m m | ce between the linear and Linear Description position displacement | angula Var. θ Δθ | r quantities Unit rad (—) rad (—) | Angular Description angle; angular position angular displacement | | |
| | corresp Var. | ondeno Unit m m s | ce between the linear and Linear Description position displacement velocity | angula Var. θ Δθ ϖ | r quantities. Unit rad (-) rad (-) $\frac{rad}{s} \left(\frac{1}{s}\right)$ | Angular Description angle; angular position angular displacement angular velocity | | |
| | corresp Var. x d,∆x | ondeno Unit m m | ce between the linear and Linear Description position displacement velocity acceleration | angula Var. θ Δθ | r quantities Unit rad (—) rad (—) | Angular Description angle; angular position angular displacement | | |
| | corresp Var. $\vec{a}, \Delta x$ \vec{v} | ondeno Unit m m s | ce between the linear and Linear Description position displacement velocity | angula Var. θ Δθ ϖ | r quantities. Unit rad (-) rad (-) $\frac{rad}{s} \left(\frac{1}{s}\right)$ | Angular Description angle; angular position angular displacement angular velocity | | |
| | corresp Var. x d,∆x v a t | ondeno Unit m m s m s ² s | ce between the linear and Linear Description position displacement velocity acceleration | angula Var. θ Δθ $\vec{\omega}$ $\vec{\alpha}$ t | r quantities. Unit rad (-) rad (-) $\frac{rad}{s} \left(\frac{1}{s}\right)$ $\frac{rad}{s^2} \left(\frac{1}{s^2}\right)$ S | Angular Description angle; angular position angular displacement angular velocity angular acceleration time | | |
| | corresp Var. x $\vec{d}, \Delta x$ \vec{v} \vec{a} t Notice to Note also | Unit m m m s ^m s ² s that ea | ce between the linear and Linear Description position displacement velocity acceleration time ch of the linear variables h "radian" is a dimensionles | angula Var. θ Δθ ϖ t as an a s quan | r quantities Unit rad (-) rad (-) $\frac{rad}{s} \left(\frac{1}{s}\right)$ $\frac{rad}{s^2} \left(\frac{1}{s^2}\right)$ s ingular courtity. A radia | Angular Description angle; angular position angular displacement angular velocity angular acceleration time time angular time angular acceleration time | | |
| | corresp Var. x $\vec{d}, \Delta x$ \vec{v} \vec{a} t Notice to an angle | ondeno Unit m m $\frac{m}{s}$ $\frac{m}{s^2}$ s that ea so that e as the | ce between the linear and Linear Description position displacement velocity acceleration time ch of the linear variables h "radian" is a dimensionles e ratio of the arc length to | angula Var. θ Δθ α t as an a s quan the rac | r quantities. Unit rad (-) rad (-) $\frac{rad}{s} (\frac{1}{s})$ $\frac{rad}{s^2} (\frac{1}{s^2})$ s ingular courtity. A radiation of the context of | Angular Description angle; angular position angular displacement angular velocity angular acceleration time hterpart. an is a ratio that describes ircle. This ratio is | | |
| | corresp Var. x $\vec{d}, \Delta x$ \vec{v} \vec{a} t Notice to Note also an angle dimension | ondeno Unit m m $\frac{m}{s}$ $\frac{m}{s^2}$ s that ea that ea that ea that ea | ce between the linear and Linear Description position displacement velocity acceleration time ch of the linear variables h "radian" is a dimensionless e ratio of the arc length to (has no unit), because the | angula Var. θ Δθ α t as an a s quan the rac | r quantities. Unit rad (-) rad (-) $\frac{rad}{s} (\frac{1}{s})$ $\frac{rad}{s^2} (\frac{1}{s^2})$ s ingular courtity. A radiation of the context of | Angular Description angle; angular position angular displacement angular velocity angular acceleration time hterpart. an is a ratio that describes ircle. This ratio is | | |
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| | corresp Var. x $\vec{d}, \Delta x$ \vec{v} \vec{a} t Notice to Note also an angle dimension | ondeno Unit m m $\frac{m}{s}$ $\frac{m}{s^2}$ s that ea that ea that ea that ea | ce between the linear and Linear Description position displacement velocity acceleration time ch of the linear variables h "radian" is a dimensionless e ratio of the arc length to (has no unit), because the | angula Var. θ Δθ α t as an a s quan the rac | r quantities. Unit rad (-) rad (-) $\frac{rad}{s} (\frac{1}{s})$ $\frac{rad}{s^2} (\frac{1}{s^2})$ s ingular courtity. A radiation of the context of | Angular Description angle; angular position angular displacement angular velocity angular acceleration time hterpart. an is a ratio that describes ircle. This ratio is | | |

Use this space for summary and/or additional notes:

Solving Linear & Rotational Motion Problems

| Big Ideas | Details | Unit: Kinematic | s (Motion) in N | Iultiple Dimensions | | | |
|-----------|---|---|----------------------|--|--|--|--|
| AP® | Of course, the same would be true if we measured angles in degrees (or gradians [*] or anything else), but using radians makes many of the calculations particularly convenient. | | | | | | |
| | We have learned the following equations for solving motion problems. Again, note the correspondence between the linear and angular equations. | | | | | | |
| | Linear Equation | Angular Equation | Relationship | Comments | | | |
| | $\vec{d} = \Delta \vec{x} = \vec{x} - \vec{x}_o$ | $\Delta \vec{\theta} = \vec{\theta} - \vec{\theta}_o$ | $s=r\Delta\theta$ | Definition of displacement. | | | |
| | $\vec{v}_{ave.} = \frac{\vec{d}}{t} = \frac{\Delta \vec{x}}{t} = \frac{\vec{v}_o + \vec{v}}{2}$ | $\vec{\boldsymbol{\omega}}_{ave.} = \frac{\Delta \vec{\boldsymbol{\theta}}}{t} = \frac{\vec{\boldsymbol{\omega}}_o + \vec{\boldsymbol{\omega}}}{2}$ | $v_{\tau} = r\omega$ | Definition of average velocity. Note that you can't use $\vec{v}_{ave.}$ or $\vec{\omega}_{ave.}$ if there is acceleration. | | | |
| | $\vec{\pmb{a}} = \frac{\Delta \vec{\pmb{v}}}{t} = \frac{\vec{\pmb{v}} - \vec{\pmb{v}}_o}{t}$ | $\vec{\alpha} = \frac{\Delta \vec{\omega}}{t} = \frac{\vec{\omega} - \vec{\omega}_o}{t}$ | $a_{\tau} = r\alpha$ | Definition of acceleration. | | | |
| | $\vec{x} - \vec{x}_o = \vec{d} = \vec{v}_o t + \frac{1}{2}\vec{a}t^2$ | $\vec{\theta} - \vec{\theta}_o = \Delta \vec{\theta} = \vec{\omega}_o t + \frac{1}{2}\vec{\alpha}t^2$ | 2 | Position/ displacement formula. | | | |
| | $ec{m{v}}^2 - ec{m{v}}_o^2 = 2ec{m{a}}ec{m{d}}$ $ec{m{v}}^2 - ec{m{v}}_o^2 = 2ec{m{a}}(\Deltaec{m{x}})$ | $\vec{\boldsymbol{\omega}}^2 - \vec{\boldsymbol{\omega}}_o^2 = 2\vec{\boldsymbol{\alpha}}\Delta\vec{\boldsymbol{\theta}}$ | | Relates velocities, acceleration and distance. Useful if time is not known. | | | |
| | $a_c = \frac{v^2}{r}$ | $a_c = r\omega^2$ | | Centripetal acceleration (toward the center of a circle.) | | | |
| | Note that vector quantities can be positive or negative, depending on direction. | | | | | | |
| | Note that \vec{r} , $\vec{\omega}$ and $\vec{\alpha}$ are vector quantities. However, the equations that relate linear and angular motion and the centripetal acceleration equations apply to magnitudes only, because of the differences in coordinate systems and changing frames of reference. | | | | | | |
| | | ote that the relationship $s = r \Delta \theta$ is not listed on the AP [®] Physics exam sheet (even nough it appears explicitly in the Course & Exam Description), so you need to nemorize it ! | | | | | |

^{*} A gradian is $\frac{9}{10}$ of a degree, which means a right angle measures 100 gradians. It is sometimes called a "metric degree" because it was introduced as part of the metric system in France in the 1790s.

Use this space for summary and/or additional notes:

Solving Linear & Rotational Motion Problems

Page: 255

| Big Ideas | Details Unit: Kin | ematics (Motion) in Multiple Dimensions | | | | | |
|-----------|--|--|--|--|--|--|--|
| AP® | Selecting the Right Equation | | | | | | |
| | (This is the same as the list from page 188, with the addition of angular velocity.) | | | | | | |
| | When you are faced with a problem, choose an equation based on the following criteria: The equation <i>must</i> contain the variable you are looking for. All other quantities in the equation must be either given in the problem or assumed from the description of the problem. | | | | | | |
| | | | | | | | |
| | | | | | | | |
| | Linear | Angular | | | | | |
| | • If an object starts at rest (not moving), then $\vec{v}_o = 0$. | • If an object's rotation starts from rest (not rotating), then $\vec{w}_o = 0$. | | | | | |
| | • If an object comes to a stop, then $\vec{v} = 0$. | • If an object stops rotating, then $\vec{\omega} = 0$. | | | | | |
| | • If an object is moving at a constant velocity, then $\vec{v} = \text{constant} = \vec{v}_{ave}$ and $\vec{a} = 0$. | • If an object is rotating at a constant rate (angular velocity), then $\vec{\omega} = \text{constant} = \vec{\omega}_{ave.}$ and $\vec{\alpha} = 0$. | | | | | |
| | • If an object is in free fall, then $\vec{a} = \vec{g} \approx 10 \frac{\text{m}}{\text{s}^2}$. | | | | | | |
| | This means you can choose the appropriate equation by making a list of what y are looking for and what you know. The equation in which you know everythin except what you are looking for is the one to use. | | | | | | |
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Use this space for summary and/or additional notes: