		Torque	Page: 364		
Big Ideas	Details		Unit: Rotational Statics & Dynamics		
	Torque				
	Unit: Rotational Statics & Dynamics				
	NGSS Standards/MA Curriculum Frameworks (2016): N/A				
	AP [®] Physics 1 Learning Objectives/Essential Knowledge (2024): 5.3.A, 5.3.A.1,				
	5.3.A.2, 5.3.B.1, 5.3.B.1, i, 5.3.B.1, ii, 5.3.B.2				
	Calculate the torque on an object				
	Calculate the location of the fullerum of a system using balanced torques				
	 Calculate the amount and distance from the fulcrum of the mass needed to balance a system. 				
	Success Criteria:				
	 Variables and 	re correctly identified and sub	ostituted correctly into equations.		
	 Equations f algebraicall 	or torques on different masse y.	es are combined correctly		
	 Algebra is c reasonable 	orrect and rounding to appro	priate number of significant figures is		
	Language Objectives:				
	 Explain why a longer lever arm is more effective. 				
	Tier 2 Vocabulary	: balance, torque			
	Labs, Activities & Demonstrations:				
	Balance an	 Balance an object on two fingers and slide both toward the center. 			
	Clever wine	e bottle stand.			
	Notes:				
	<u>torque</u> (₹): a vec rotation. Tak Torque is mea	ctor quantity that measures the care to distinguish the Gree asured in units of newton-me	he effectiveness of a force in causing ek letter " $ au$ " from the Roman letter "t". ters:		
		$1N \cdot m = 1 \frac{kg}{k}$	5 ^{cm2} / _{5²}		
	Note that wo newton-mete torque, and a energy are sc	rk and energy (which we will ers. However, work and energers not interchangeable. (Amealar quantities, and torque is	study later) are also measured in gy are different quantities from ong other differences, work and a vector quantity.)		
	axis of rotation: the point around which an object rotates.				
	fulcrum: the point around which a lever pivots. Also called the pivot.				
	lever arm: the distance from the axis of rotation that a force is applied, causing a torque.				
	Use this space for	summary and/or additional	notes:		

		Torque		Page: 365	
Big Ideas	Details	•	Unit: Rotational Sta	tics & Dynamics	
	Just as force is the quantither that causes a change in the	Just as force is the quantity that causes linear acceleration, torque is the quantity that causes a change in the speed of rotation (rotational acceleration).			
	Because inertia is a property of mass, Newton's second law is the relationship between force and inertia. Newton's second law in rotational systems looks similar to Newton's second law in linear systems:				
	$\vec{a} = \frac{\sum \vec{F}}{m} = \frac{\vec{F}}{m}$: <u>net</u> M	$\vec{\alpha} = \frac{\Sigma \vec{\tau}}{I} = \frac{\vec{\tau}_{ne}}{I}$	<u>t</u>	
	$\vec{F}_{net} = m\vec{a}$		$\vec{\tau}_{net} = I \vec{\alpha}^*$		
	linear		rotational		
	As you should remember, a net force of zero, that means all forces cancel in all directions and there is no acceleration. If there is no acceleration $(\vec{a} = 0)$, the velocity remains constant (which may or may not equal zero). Similarly, if the net torque is zero, then the torques cancel in all directions and t is no angular acceleration. If there is no angular acceleration $(\vec{\alpha} = 0)$, then the angular velocity remains constant (which may or may not equal zero). rotational equilibrium : when all of the torques on an object cancel each other's effects (resulting in a net force of zero) and the object either does not rotate rotates with a constant angular velocity. Torque is also the cross product of distance from the center of rotation ("lever arm") × force:				
	$\vec{\tau} = \vec{r} \times$	F which gives:	$\ \vec{\mathbf{\tau}}\ = \tau = rF\sin\theta = rF_{\perp}$		
	where $ heta$ is the angle between the lever arm and the applied force.				
	We use the variable <i>r</i> for the lever arm (which is a distance) because torque causes rotation, and <i>r</i> is the distance from the center of the circle (radius) at which the force is applied.				
	$F\sin\theta$ is sometimes written as F_{\perp} (the component of the force that is perpendicular				
	to the radius) and sometimes $F_{ }$ (the component of the force that is parallel to the				
	direction of motion). These notes will use ${\it F}_{\!\scriptscriptstyle \perp}$, because in many cases the force is				
	applied to a lever, and the component of the force that causes the torque is perpendicular to the lever itself, so it is easy to think of it as "the amount of force that is perpendicular to the lever". This gives the equation:				
	$ au = rF_{\perp}$				
	* In this equation, $\bar{\alpha}$ is angular acceleration, which is studied in AP [®] Physics 1, but is beyond the scope of the CP1 and honors physics course. Qualitatively, angular acceleration is a change in how fast something is rotating.				

Details

Seesaw Problems

A seesaw problem is one in which objects on opposite sides of a lever (such as a seesaw) balance one another.

To solve seesaw problems, if the seesaw is not moving, then the torques must balance and the net torque must be zero.

The total torque on each side is the sum of the separate torques caused by the separate masses. Each of these masses can be considered as a point mass (infinitely small object) placed at the object's *center of mass*.

Sample Problems:

Q: A 100 cm meter stick is balanced at its center (the 50-cm mark) with two objects hanging from it, as shown below:



One of the objects weighs 4.5 N, and is hung from the 20-cm mark (30 cm = 0.3 m from the fulcrum). A second object is hung at the opposite end (50 cm = 0.5 m from the fulcrum). What is the weight of the second object?

A: In order for the ruler to balance, the torque on the left side (which is trying to rotate the ruler counter-clockwise) must be equal to the torque on the right side (which is trying to rotate the ruler clockwise). The torques from the two halves of the ruler are the same (because the ruler is balanced in the middle), so this means the torques applied by the objects also must be equal.

The torque applied by the object on the left is:

$$\tau = rF = (0.30)(4.5) = 1.35 \,\mathrm{N} \cdot \mathrm{m}$$

The torque applied by the object on the right must also be 1.35 N·m, so we can calculate the force:

$$\tau = rF$$

1.35 = 0.50F
 $F = \frac{1.35}{0.50} = 2.7 \,\mathrm{N}$



Torque

Big Ideas	Details	Unit: Rotational Statics & Dynamics			
honors & AP®	Left Side (CCW = び)	Right Side (CW = 신)			
	Person	Person			
	The person has a mass of 90 kg and is sitting at a distance x from the fulcrum: $\tau_{12} = rF$	The person on the right has a mass of 50 kg and is sitting at a distance of 6 – x from the fulcrum:			
	$\tau_{LP} = r(ma) - r(90 kg)(10^{ m})$	$ au_{\scriptscriptstyle RP} = rF$			
	$t_{LP} = X(Hg) = X(90 \text{ kg})(10 \frac{1}{s^2})$	$\tau_{RP} = r(mg) = (6 - x)(50 \text{ kg})(10 \frac{\text{m}}{2})$			
	$i_{LP} = 900x$	$\tau_{pp} = 500 (6 - x)$			
	Baard	$\tau_{RP} = 3000 - 500x$			
	Board The center of mass of the left part of the	Board			
	here the of mass of the left part of the	The center of mass of the right part of the board is at a distance of $\frac{6-x}{2}$.			
	The weight (F_g) of the board to the left of the fulcrum is $\left(\frac{x}{6}\right)$ (20)(10)				
		The weight (F_{e}) of the board to the right			
		of the fulcrum is $\left(\frac{6-x}{c}\right)$ (20)(10)			
	$\tau_{LB} = rF$	$\tau_{\rm op} = rF$			
	$\tau_{LB} = r(mg) = \left(\frac{x}{2}\right) \left(\frac{x}{6.0}\right) (20) (10)$	$\tau = r(mq) = (\frac{6-x}{2})(\frac{6-x}{2})(20)(10)$			
	$\tau_{LB} = 16.\overline{6} x^2$	$r_{RB} = r(r_{RB})^{-1} (2) (6) (20) (10)$			
		$\tau_{RB} = 16.6 (36 - 12x + x^{-})$			
	Total	$\tau_{RB} = 600 - 200x + 16.6x$			
	$\tau_{\rm ccw} = \tau_{\rm LB} + \tau_{\rm LP}$	Total			
	$\tau_{ccw} = 16.\overline{6}x^2 + 900x$	$\tau_{cw} = \tau_{RB} + \tau_{RP}$			
		$\tau_{cw} = 16.6x^2 - 200x + 600 + 3000 - 500x$			
		$\tau_{cw} = 16.6x^2 - 700x + 3600$			
	Because the seesaw is not rotating, the net torque must be zero. So we need to define the positive and negative directions. A common convention is to define counter-clockwise as the positive direction. (Most math classes already do this—a positive angle means counter-clockwise starting from zero at the <i>x</i> -axis.)				
	This gives:				
	$\tau_{ccw} = 16.\overline{6}x^2 + 900x \qquad \tau_{cw} = -(16.\overline{6}x^2)^2$	$-700x+3600) = -16.\overline{6}x^2+700x-3600$			



Use this space for summary and/or additional notes:



Use this space for summary and/or additional notes:

		Torque Page: 372
Big Ideas	Details	Unit: Rotational Statics & Dynamics
	5.	(M) In the following diagram, a meter stick is balanced in the center (at the 50 cm mark). A 6.2 N weight is hung from the meter stick at the 30 cm mark. How much weight must be hung at the 100 cm mark in order to balance the meter stick?
		<u>20 30 40 60 30 100</u> <u>6.2 N</u> <i>X</i> Hints:
		• The meter stick has the same amount of mass on both sides of the fulcrum. This means it applies the same amount of torque in both directions and you don't need to include it in your calculations.
		 The 30 cm mark is 20 cm = 0.2 m from the fulcrum; the 100 cm mark is 50 cm = 0.5 m from the fulcrum.
		Answer: 0.25 kg
honors & AP®	6.	(M – AP®; S – honors; A – CP1) The seesaw shown in the following diagram balances when no one is sitting on it. The child on the right has a mass of 35 kg and is sitting 2.0 m from the fulcrum. If the adult on the left has a mass of 85 kg, how far should the adult sit from the fulcrum in order for the seesaw to be balanced?
I		Answer: 0.82 m

Use this space for summary and/or additional notes: