Conservation of Energy

Unit: Energy, Work & Power

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS3-1

AP® Physics 1 Learning Objectives/Essential Knowledge (2024): 3.4.A, 3.4.A.1, 3.4.A.2, 3.4.B, 3.4.B.1, 3.4.B.2, 3.4.B.3, 3.4.B.4, 3.4.C, 3.4.C.1, 3.4.C.2, 3.4.C.3

Mastery Objective(s): (Students will be able to…)

• Solve problems that involve the conversion of energy from one form to another.

Success Criteria:

- Correct equations are chosen for the situation.
- Variables are correctly identified and substituted correctly into equations.
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

Language Objectives:

• Describe the type(s) of energy that an object has in different situations.

Tier 2 Vocabulary: work, energy, potential

Labs, Activities & Demonstrations:

- Golf ball loop-the-loop.
- Marble raceways.
- Bowling ball pendulum.

Notes:

In a *closed system* (meaning a system in which there is no exchange of matter or energy between the system and the surroundings), the total energy is constant. Energy can be converted from one form to another. When this happens, the increase in any one form of energy is the result of a corresponding decrease in another form of energy.

mechanical energy: kinetic energy plus gravitational potential energy.

In a system that has potential energy and kinetic energy, the total mechanical energy is given by:

$TMF = U + K$

If there is no work done on a system and there are no nonconservative interactions, then the total mechanical energy of the system is constant.

Conservation of Energy Page: 460 Big Ideas Details Details Details Details Details Details Details Unit: Energy, Work & Power In the following diagram, suppose that a student drops a ball with a mass of 2 kg from a height of 3 m. $U_a = 30 J$ $U_g = 60 J$ $K = 60$ J $K = 30J$ potential potential energy kinetic energy being converted to energy only kinetic energy only Before the student lets go of the ball, it has 60 J of potential energy. As the ball falls to the ground, potential energy is gradually converted to kinetic energy. The potential energy continuously decreases and the kinetic energy continuously increases, but the total energy is always 60 J. After the ball hits the ground, 60 J of work was done by gravity, and the 60 J of kinetic energy is converted to other forms. For example, if the ball bounces back up, some of the kinetic energy is converted back to potential energy. If the ball does not reach its original height, that means the rest of the energy was converted into other forms, such as thermal energy (the temperatures of the ball and the ground increase infinitesimally), sound, *etc.*

Conservation of Energy

In physics, if a quantity is "conserved", that means when some change happens to a system, there is the same amount of that quantity after the change as there was before.

Energy Bar Charts

A useful way to represent conservation of energy is through bar graphs that represent kinetic energy (*K* or "KE"), gravitational potential energy (*U^g* or "PE"), and total mechanical energy (TME). (We use the term "chart" rather than "graph" because the scale is usually arbitrary and the chart is not meant to be used quantitatively.)

The following is an energy bar chart for a roller coaster, starting from point A and traveling through points B, C, D, and E.

Notice, in this example, that:

- 1. The total mechanical energy always remains the same. (This the case in conservation of energy problems if there is no work added to or removed from the system.)
- 2. KE is zero at point **A** because the roller coaster is not moving. All of the energy is PE, so PE = TME.
- 3. PE is zero at point **D** because the roller coaster is at its lowest point. All of the energy is KE, so KE = TME.
- 4. At all points (including points **A** and **D**), KE + PE = TME

It can be helpful to sketch energy bar charts representing the different points in complicated conservation of energy problems. If energy is being added to or removed from the system, add an Energy Flow diagram to show energy that is being added to or removed from the system.

Typically, energy bar charts represent the initial ("before") and final ("after") mechanical energy as a bar graph, and we represent the system in the center as a circle with work available to go in or out ("change").

For example, suppose a car started out moving (which means it started with kinetic energy or KE) and was at the top of a hill (which means it started with gravitational potential energy or GPE). The car ended up on top of a higher hill (which means it ended with more GPE), and was also going faster (which means it also ended with more KE). In order to make the car speed up while it was also going up a hill, the driver had to press the accelerator, causing the engine to do work. The energy bar chart diagram would look like this:

Notice that:

- The initial GPE and initial KE add up to the initial total mechanical energy (T.M.E.).
- The initial T.M.E. plus the work adds up to the final T.M.E.
- The final GPE and final K add up to the final T.M.E.
- The conservation equation is $U_{g,o} + K_o + W = U_g + K$

Charts like this are called "LOL charts" or "LOL diagrams," because the axes on the left and right side resemble the letter "L", and the circle for the system resembles the letter "O".

Once you have the types of energy, replace each type of energy with its equation:

- $W = F \cdot d = Fd \cos \theta$ (= *Fd* if force & displacement are in the same direction)
- $U_q = mgh$
- 1 ² $K = \frac{1}{2}mv$

For this problem, the equation would become:

$$
U_{g,o} + K_o + W = U_g + K
$$

$$
mgh_o + \frac{1}{2}mv_o^2 + W = mgh + \frac{1}{2}mv^2
$$

In most problems, one or more of these quantities will be zero, making the problem easier to solve.

Big Ideas Details Details Details Details Big Ideas Details Unit: Energy, Work & Power Q: An 80 kg physics student falls off the roof of a 15 m high school building. How much kinetic energy does he have when he hits the ground? What is his final velocity? A: There are two approaches to answer this question. 1. Recognize that the student's potential energy at the top of the building is entirely converted to kinetic energy when he hits the ground. **Initial** $\ddot{}$ Change **Final** \blacksquare conservation of energy T.M.E. T.M.E. K $U_{q,0}$ + У. ÷ W \blacksquare X, $\ddot{}$ *Notice that:* • *No work is done on the student[.](#page-6-0)* Total mechanical energy therefore is the same at the beginning and end.* • *Initially, the student has only gravitational potential energy. At the end, the student has no potential energy and all of his energy has been converted to kinetic. g o U K* = , 2 1 $mgh_o = \frac{1}{2}mv$ 1 (2001.2) (80)(10)(15) = $\frac{1}{2}$ (80)*v* $12000 = 40v^2$ $\frac{12000}{40} = 300 = v^2$ $v = \sqrt{300} = 17.3 \frac{m}{s}$ $=40v^2$ $\frac{1}{40}$ $=300 = v^2$ $v = \sqrt{300}$ $=$ Answers: $K_f = 12\,000 \text{ J}$; $v_f = 17.3 \frac{\text{m}}{\text{s}}$ Actually, we have two options. If we consider the Earth-student system, no outside energy is added or removed, which means there is no work, and gravitational potential energy is converted to kinetic energy. If we consider the student-only system, then there is no potential energy, and gravity does work on the student to increase their kinetic energy: $W = F_g \bullet d = mgh$. The two situations are equivalent and give the same answer.

