Unit: Energy, Work & Power

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS3-1

AP<sup>®</sup> Physics 1 Learning Objectives/Essential Knowledge (2024): 3.4.A, 3.4.A.1, 3.4.A.2, 3.4.B, 3.4.B.1, 3.4.B.2, 3.4.B.3, 3.4.B.4, 3.4.C, 3.4.C.1, 3.4.C.2, 3.4.C.3

Mastery Objective(s): (Students will be able to...)

• Solve problems that involve the conversion of energy from one form to another.

### Success Criteria:

- Correct equations are chosen for the situation.
- Variables are correctly identified and substituted correctly into equations.
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

#### Language Objectives:

• Describe the type(s) of energy that an object has in different situations.

Tier 2 Vocabulary: work, energy, potential

### Labs, Activities & Demonstrations:

- Golf ball loop-the-loop.
- Marble raceways.
- Bowling ball pendulum.

### Notes:

In a *closed system* (meaning a system in which there is no exchange of matter or energy between the system and the surroundings), the total energy is constant. Energy can be converted from one form to another. When this happens, the increase in any one form of energy is the result of a corresponding decrease in another form of energy.

mechanical energy: kinetic energy plus gravitational potential energy.

In a system that has potential energy and kinetic energy, the total mechanical energy is given by:

#### TME = U + K

If there is no work done on a system and there are no nonconservative interactions, then the total mechanical energy of the system is constant.



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	Work-Energy Theorem
	We have already seen that work is the action of a force applied over a distance. A broader and more useful definition is that work is the change in the energy of an object or system. If we think of a system as having imaginary boundaries, then work is the flow of energy across those boundaries, either into or out of the system.
	For a system that has only mechanical energy, work changes the amount of potential and/or kinetic energy in the system.
	$W = \Delta K + \Delta U$
	As mentioned earlier, although work is a scalar quantity, we <b>use generally use a positive number for work coming into the system</b> ("work is done on the system"), and <b>a negative number for work going out of the system</b> ("work is done by the system on the surroundings").
	The units for work are sometimes shown as newton-meters ( $N \cdot m$ ). Because work is equivalent to energy, the units for work and energy—newton-meters and joules—are equivalent.
	$1J\!\equiv\!1N\!\cdot\!m\!\equiv\!1\frac{kg\cdot m^2}{s^2}$
	Work-energy theorem problems will give you information related to the gravitational potential and/or kinetic energy of an object (such as its mass and a change in velocity) and ask you how much work was done.
	A simple rule of thumb (meaning that it's helpful, though not always strictly true) is:
	• Potential energy is energy in the <i>future</i> (energy that is available for use).
	<ul> <li>Kinetic energy is energy in the <i>present</i> (the energy of an object that is currently in motion).</li> </ul>
	<ul> <li>Work is the result of energy in the <i>past</i> (energy that has already been added to or taken from an object).</li> </ul>

Details

## **Conservation of Energy**

In physics, if a quantity is "conserved", that means when some change happens to a system, there is the same amount of that quantity after the change as there was before.

### **Energy Bar Charts**

A useful way to represent conservation of energy is through bar graphs that represent kinetic energy (K or "KE"), gravitational potential energy ( $U_g$  or "PE"), and total mechanical energy (TME). (We use the term "chart" rather than "graph" because the scale is usually arbitrary and the chart is not meant to be used quantitatively.)

The following is an energy bar chart for a roller coaster, starting from point A and traveling through points B, C, D, and E.



Notice, in this example, that:

- 1. The total mechanical energy always remains the same. (This the case in conservation of energy problems if there is no work added to or removed from the system.)
- 2. KE is zero at point **A** because the roller coaster is not moving. All of the energy is PE, so PE = TME.
- 3. PE is zero at point **D** because the roller coaster is at its lowest point. All of the energy is KE, so KE = TME.
- 4. At all points (including points A and D), KE + PE = TME

It can be helpful to sketch energy bar charts representing the different points in complicated conservation of energy problems. If energy is being added to or removed from the system, add an Energy Flow diagram to show energy that is being added to or removed from the system.

Typically, energy bar charts represent the initial ("before") and final ("after") mechanical energy as a bar graph, and we represent the system in the center as a circle with work available to go in or out ("change").

For example, suppose a car started out moving (which means it started with kinetic energy or KE) and was at the top of a hill (which means it started with gravitational potential energy or GPE). The car ended up on top of a higher hill (which means it ended with more GPE), and was also going faster (which means it also ended with more KE). In order to make the car speed up while it was also going up a hill, the driver had to press the accelerator, causing the engine to do work. The energy bar chart diagram would look like this:



Notice that:

**Big Ideas** 

Details

- The initial GPE and initial KE add up to the initial total mechanical energy (T.M.E.).
- The initial T.M.E. plus the work adds up to the final T.M.E.
- The final GPE and final K add up to the final T.M.E.
- The conservation equation is  $U_{a,o} + K_o + W = U_a + K$

Charts like this are called "LOL charts" or "LOL diagrams," because the axes on the left and right side resemble the letter "L", and the circle for the system resembles the letter "O".

Once you have the types of energy, replace each type of energy with its equation:

- $W = F \bullet d = Fd \cos \theta$  (= Fd if force & displacement are in the same direction)
- $U_a = mgh$
- $K = \frac{1}{2}mv^2$

For this problem, the equation would become:

$$U_{g,o} + K_o + W = U_g + K$$
$$mgh_o + \frac{1}{2}mv_o^2 + W = mgh + \frac{1}{2}mv^2$$

In most problems, one or more of these quantities will be zero, making the problem easier to solve.





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	2. You can also use motion equations to find the student's velocity when he hits the ground, based on the height of the building and acceleration due to			
	gravit	y. Then use the formula $K =$	$=\frac{1}{2}mv^2.$	
		$d=\frac{1}{2}at^2$		
		$15=\frac{1}{2}(10)t^2$	$K = \frac{1}{2}mv^2$	
		$t^2 = 3$	$K = \frac{1}{2}(80)(17.32)^2$	
		$t = \sqrt{3} = 1.732$	K = 12000 J	
		v = 0.0 $v = (10)(1.732) = 17.32 \frac{n}{s}$	1	
	Answers: $K_f = 12000 \text{ J}$ ; $v_f = 17.3 \frac{\text{m}}{\text{s}}$ as before.			
	1			







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	6.	<b>(S)</b> The 10. N fo	e engine of a 0.200 kg model rocket provides a constant thrust of or 1.0 s.
		a.	(S) What is the net force that the engine applies to the rocket? ( <i>Hint: This is a forces problem. Draw a free-body diagram.</i> )
			Answer: 8.0 N
		b.	<b>(S)</b> What is the velocity of the rocket when the engine shuts off? What is its height at that time?
			(Hint: Use $F_{net} = ma$ to find the acceleration. Then use motion equations to find the velocity and height.)
			Answer: $v = 40.\frac{m}{s}$ ; $h = 20. m$
		с.	(S) What is the final height of the rocket?
			(Hint: calculate the kinetic energy of the rocket when the engine shuts off. This will become additional potential energy when the rocket reaches its highest point. Add this to the work from part b above to get the total energy at the end, which is all potential. Finally, use $U_g = mgh$ to find the height.)
		d.	Answer: 100 m (S) How much work did the engine do on the rocket?
			Answer: 200 N·m