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Unit: Energy, Work & Power

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Power

Unit: Energy, Work & Power

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP Physics 1 Learning Objectives/Essential Knowledge (2024): 3.5.A, 3.5.A.1,

3.5.A.2, 3.5.A.3, 3.5.A.4

Mastery Objective(s): (Students will be able to...)

• Calculate power as a rate of energy consumption.

Success Criteria:

- Variables are correctly identified and substituted correctly into the appropriate equations.
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

Language Objectives:

• Explain the difference between total energy and power.

Tier 2 Vocabulary: power

Notes:

<u>power</u>: a measure of the rate at which energy is applied or work is done. The average power is calculated by dividing work (or energy) by time.

$$P_{avg} = \frac{\Delta E}{t} = \frac{W}{t} = \frac{\Delta K + \Delta U}{t}$$

Power is a scalar quantity and is measured in Watts (W).

$$1W = 1\frac{J}{s} = 1\frac{N \cdot m}{s} = 1\frac{kg \cdot m^2}{s^3}$$

Note that utility companies measure energy in kilowatt-hours. This is because

$$P = \frac{W}{t}$$
, which means energy = $W = Pt$.

Because 1 kW = 1000 W and 1 h = 3600 s, this means

1 kWh = (1000 W)(3600 s) = 3600000 J

Because
$$W = F_{\parallel}d$$
, this means $P_{avg} = \frac{F_{\parallel}d}{t} = F_{\parallel}\left(\frac{d}{t}\right) = F_{\parallel}v_{avg}$

However, if we use the instantaneous velocity instead of the average velocity, this equation gives us the instantaneous power:

$$P_{inst} = F_{\parallel} v = F v \cos \theta$$

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 ΔP^{\otimes}

Power in Rotational Systems

In a rotational system, the formula for power looks similar to the equation for power in linear systems, with force replaced by torque and linear velocity replaced by angular velocity:

$$P = Fv$$
 $P = \tau \omega$ linear rotational

Solving Power Problems

Many power problems require you to calculate the amount of work done or the change in energy, which you should recall is:

$$W = F_{||} d$$
 if the force is caused by linear displacement
$$\Delta K_t = \frac{1}{2} m v^2 - \frac{1}{2} m v_o^2$$
 if the change in energy was caused by a change in velocity
$$\Delta U_g = mgh - mgh_o$$
 if the change in energy was caused by a change in height

Solving Rotational Power Problems

 AP^{\otimes}

Power is also applicable to rotating systems:

$$W = \tau \Delta \theta$$
 if the work is produced by a torque
$$\Delta K_r = \frac{1}{2} I \omega^2 - \frac{1}{2} I \omega_o^2$$
 if the change in energy was caused by a change in angular velocity

Once you have the work or energy, you can plug it in for either W, ΔK or ΔU , use the appropriate parts of the formula:

$$P = \frac{W}{t} = \frac{\Delta K + \Delta U}{t} = Fv = \tau \omega$$

and solve for the missing variable.

^{*} K_t is translational kinetic energy. This is the only form of kinetic energy used in CP1 and honors physics. The subscript t is used here to distinguish translational kinetic energy from rotational kinetic energy (K_r), because both are used in AP® Physics.

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Sample Problems:

Q: What is the power output of an engine that pulls with a force of 500. N over a distance of 100. m in 25 s?

A:
$$W = Fd = (500)(100) = 50000 \text{ J}$$

$$P = \frac{W}{t} = \frac{50000}{25} = 2000 \text{ W}$$

Q: A 60. W incandescent light bulb is powered by a generator that is powered by a falling 1.0 kg mass on a rope. Assuming the generator is 100% efficient (i.e., no energy is lost when the generator converts its motion to electricity), how far must the mass fall in order to power the bulb at full brightness for 1.0 minute?

A:
$$P = \frac{\Delta U_g}{t} = \frac{mg \, \Delta h}{t}$$
$$60 = \frac{(1)(10) \, \Delta h}{60}$$
$$3600 = 10 \, \Delta h$$
$$\Delta h = \frac{3600}{10} = 360 \, \text{m}$$

Note that 360 m is approximately the height of the Empire State Building. This is why changing from incandescent light bulbs to more efficient compact fluorescent or LED bulbs can make a significant difference in energy consumption!

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Homework Problems

1. (S) A small snowmobile has a 9000 W (12 hp) engine. It takes a force of 300. N to move a sled load of wood along a pond. How much time will it take to tow the wood across the pond if the distance is measured to be 850 m?

Answer: 28.3 s

Big Ideas

Details

2. (M) A winch, which is rated at 720 W, is used to pull an all-terrain vehicle (ATV) out of a mud bog for a distance of 2.3 m. If the average force applied by the winch is 1500 N, how long will the job take?

Answer: 4.8 s

3. (S) What is your power output if you have a mass of 65 kg and you climb a 5.2 m vertical ladder in 10.4 s?

Answer: 325 W

- 4. (M) Jack and Jill went up the hill. (The hill was 23m high.) Jack was carrying a 21 kg pail of water.
 - a. (M) Jack has a mass of 75 kg and he carried the pail up the hill in 45 s. How much power did he apply?

Answer: 490.7 W

b. (M) Jill has a mass of 55 kg, and she carried the pail up the hill in 35 s. How much power did she apply?

Answer: 499.4 W

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honors & AP®

5. **(M – honors & AP®; A – CP1)** The maximum power output of a particular crane is P. What is the fastest time, t, in which this crane could lift a crate with mass m to a height h?

(If you are not sure how to do this problem, do #6 below and use the steps to guide your algebra.)

Answer:
$$t = \frac{mgh}{P}$$

6. **(S – honors & AP®; M – CP1)** The maximum power output of a particular crane is 12 kW. What is the fastest time in which this crane could lift a 3500 kg crate to a height of 6.0 m?

(<u>You must start with the equations in your Physics Reference Tables and show all of the steps of GUESS.</u> You may only use the answer to question #5 above as a starting point if you have already solved that problem.)

Hint: Remember to convert kilowatts to watts.

Answer: 17.5 s

 $AP^{@}$

- 7. **(M AP®; A honors & CP1)** A 30 cm diameter solid cylindrical flywheel with a mass of 2 500 kg was accelerated from rest to an angular velocity of 1800 RPM in 60 s.
 - a. How much work was done on the flywheel?

Answer: 5.0×10⁵ N⋅m

b. How much power was exerted?

Answer: 8.3×10³ W