## Simple Harmonic Motion Page: 526 **Big Ideas** Details Unit: Simple Harmonic Motion Simple Harmonic Motion Unit: Simple Harmonic Motion NGSS Standards/MA Curriculum Frameworks (2016): N/A AP® Physics 1 Learning Objectives/Essential Knowledge (2024): 7.1.A, 7.1.A.1, 7.1.A.2, 7.1.A.2.i, 7.1.A.2.ii, 7.1.A.2.iii, 7.2.A, 7.2.A.1, 7.2.A.1.i, 7.2.A.1.ii, 7.3.A, 7.3.A.1, 7.3.A.1.i, 7.3.A.1.ii, 7.3.A.2, 7.3.A.3 Mastery Objective(s): (Students will be able to...) • Describe simple harmonic motion and explain the behaviors of oscillating systems such as springs & pendulums. **Success Criteria:** • Explanations are sufficient to predict the observed behavior. Language Objectives: • Explain why oscillating systems move back and forth by themselves. Tier 2 Vocabulary: simple, harmonic Labs, Activities & Demonstrations: Show & tell with springs & pendulums. Notes: simple harmonic motion: motion consisting of regular, periodic back-and-forth oscillation. restoring force: a force that pushes or pulls an object in SHM toward its equilibrium position. equilibrium position: a point in the center of an object's oscillation where the net force on the object is zero. If an object is placed at the equilibrium position with a velocity of zero, the object will remain there. Because the restoring force is in the opposite direction from the displacement, acceleration is also in the opposite direction from displacement. This means the acceleration always slows down the motion and reverses the direction. Applying Netwon's Second Law gives $m\vec{a}_{x} = -k\Delta\vec{x}$ . In this equation, k is an arbitrary constant that makes the units work. The units of this constant are $\frac{N}{m}$ .



## Simple Harmonic Motion





**Big Ideas** 

Details

Kinematics of Simple Harmonic Motion
As described above, the y-position of an object in simple harmonic motion as a function of time is the sine or cosine of an angle around the unit circle.
From the rotational kinematics equations (in the <i>Solving Linear &amp; Rotational Motion Problems</i> topic starting on page 253), the object's change in position is given by the equation $\Delta \theta = \omega t$ . Because the object's angular starting position is arbitrary, we can describe this starting position by anoffset angle, $\phi$ . This angle is called the <i>phase</i> .
We can therefore describe the object's position using the equation:
position: $x = A\cos(\omega t + \phi)$
From calculus, because velocity is the first derivative of position with resect to time and acceleration is the second derivative, the general equations for periodic motion are therefore:
velocity: $v = -A\omega \sin(\omega t + \phi) = \frac{dx}{dt}^*$
acceleration: $a = -A\omega^2 \cos(\omega t + \phi) = \frac{dv}{dt} = \frac{d^2x}{dt^2}$
Because many simple harmonic motion problems (including AP <sup>®</sup> problems) are given in terms of the frequency of oscillation (number of oscillations per second), we can multiply the angular frequency by $2\pi$ (because one complete oscillation represents the distance around the unit circle) to use <i>f</i> instead of $\omega$ , <i>i.e.</i> , $\omega = 2\pi f$ .
On the AP® formula sheet, $\phi$ is assumed to be zero, which results in the following versions of the position equation:
$x = A\cos(2\pi ft)$ or $x = A\sin(2\pi ft)$
On the AP <sup>®</sup> exam, you are expected to understand and use the position equation above, but simple harmonic problems that involve the velocity and acceleration equations are beyond the scope of this course.
$dx dv d^2x$

\* The derivatives  $\frac{dx}{dt}$ ,  $\frac{dv}{dt}$ , and  $\frac{d^2x}{dt^2}$  are from calculus. The velocity and acceleration equations of SHM are beyond the scope of the AP<sup>®</sup> Physics course.

Big Ideas	Details Unit:	Simple Harmonic Motion	
	Energy in SHM		
	As in other situations, the total mechanical energy of a syst kinetic energy:	em is its potential plus	
	$E_{total} = U + K$		
	<ul> <li>In an oscillating system:</li> <li>As the restoring force moves the object toward the equilibrium position, potential energy decreases and kinetic energy increases.</li> </ul>		
	<ul> <li>The system's potential energy is at a minimum when i maximum.</li> </ul>	ts kinetic energy is at a	
	<ul> <li>As the restoring force moves the object away from the potential energy increases and kinetic energy decreas</li> </ul>	e equilibrium position, es.	
	<ul> <li>The system's kinetic energy is at a minimum when its maximum.</li> </ul>	potential energy is at a	