Thermodynamics

Unit: Thermodynamics

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-6

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 9.3.A, 9.3.A.4, 9.4.A, 9.4.A.1, 9.4.A.1.i, 9.4.A.1.ii, 9.4.A.2, 9.4.B, 9.4.B.1, 9.4.B.1.i, 9.4.B.1.ii, 9.4.B.1.iii, 9.6.A, 9.6.A.1, 9.6.A.2, 9.6.A.2.i, 9.6.A.2.iii, 9.6.A.3, 9.6.A.3.i, 9.6.A.3.ii

Mastery Objective(s): (Students will be able to…)

• Calculate kinetic energy, internal energy and work done by the particles of a gas.

Success Criteria:

- Solutions have the correct quantities substituted for the correct variables.
- Algebra and rounding to appropriate number of significant figures is correct.

Language Objectives:

• Describe the different types of energy (kinetic, internal, work) and explain what they measure.

Tier 2 Vocabulary: internal, energy, work

Labs, Activities & Demonstrations:

- heat exchange dice game
- dice distribution game
- entropy (microstates) percentile dice game

Notes:

thermodynamics: the study of heat-related (thermal) energy changes (dynamics)

Thermodynamics is an application of the law of conservation of energy. In Physics 1, we studied changes between gravitational potential energy and kinetic energy. Thermodynamic changes involve the same principle; the details and the equations, however, are quite different.

As was the case with gas laws, the topic of thermodynamics is studied by both chemists and physicists. Chemists tend to be more concerned with the heat produced and consumed by chemical changes and reactions. Physicists tend to be more concerned with the conversion between thermal energy (regardless of how it is produced) and other forms of energy, particularly mechanical.

internal energy (U^{*}[\)](#page-2-0): the total thermal energy of a system due to the kinetic energy of its particles. If the kinetic energy of a single particle is $K_{ave.} = \frac{3}{2} k_B T$, then the total kinetic

energy in a system that has *N* particles would be:

$$
U = NK_{ave.} = \frac{3}{2} N k_B T
$$

Because it is generally unwieldy to perform calculations for systems with large numbers of particles, it is more convenient to use moles. Substituting *nR* for *Nk^B* gives the equation for the internal energy of a system that has *n* moles of particles:

$$
U=\frac{3}{2}nRT
$$

Similarly, a *change* in internal energy (Δ*U*) is related to the corresponding *change* in temperature (Δ*T*):

$$
\Delta U = \frac{3}{2} n R \Delta T \ \left(= \frac{3}{2} N k_B \Delta T \right)
$$

heat (*Q*): thermal energy transferred into or out of a system. (J)

work (*W*): mechanical energy (such as the application of a force over a distance) transferred into or out of a system. (J)

The work that a gas can do comes from its ability to move an object by applying a force on it as it expands. If the pressure is constant:

$$
W = Fd = F\Delta x
$$

\n
$$
P = \frac{F}{A} \rightarrow F = PA
$$

\n
$$
\therefore W = (PA)\Delta x
$$

\n
$$
\Delta V = A\Delta x
$$

\n
$$
\therefore W = P\Delta V
$$

If a gas does work by expanding, the energy is transferred from the gas (the system) to the object that the gas is pushing against (the surroundings). This means that when the volume increases (Δ*V* is positive), energy is leaving the system (*W* is negative). Conversely, if work is done to compress a gas, energy is entering the system in order to compress the gas (*W* is positive), and the volume decreases (Δ*V* is negative). This means that *W* and *PΔV* must have opposite signs, which gives the equation:

$$
W = -P\Delta V
$$

assuming that pressure is constant.

* Chemistry textbooks often use the variable *E* instead of *U*.

Alternatively, we could calculate the work using $W = -P\Delta V$, but we would need to use gauge pressure rather than absolute pressure. (See the explanation below.)

The first two steps are the same as above.

- 1. This step is the same as step #1 above—we need to find the temperature change necessary to produce the change in volume.
- 2. This step is the same as step #2 above—we need to calculate the change in internal energy of the gas caused by the change in temperature.
- 3. Instead of calculating the work using equations from physics 1, we can use *W* =−P∆V . However, pressure needs to be the amount of pressure that is doing the work, which is the difference in pressure between the inside of the piston and the outside of the piston. (This would be the gauge pressure inside the cylinder.) We can calculate this using the pressure equation from fluids in physics 1:

$$
P = \frac{F}{A} = \frac{(2)(10)}{0.01} = 2\,000\,\text{Pa}
$$

This is the pressure at which the gas needs to do work.

Once we have the pressure, the work is given by:

 ΔV = 0.040 $-$ 0.033 = 0.007 m^{3} *W* =−(2000)(0.007) =−14 J *W* =−P∆V

4. Once we have ΔU and W, we can find Q by applying the first law:

$$
\Delta U = Q + W
$$

$$
1301 = Q + (-14)
$$

$$
1315 J = Q
$$

If the heat could be transferred in a way that is completely reversible (which is impossible and would take an infinite amount of time), then you would be able to recover the energy that was converted to entropy when transferring it back to the hotter object. We call this fictitious heat "reversible heat," denoted *Qrev*.

honors (not AP®)

 $\Delta S = \frac{Q_{rev}}{Q}$ *T*

Real energy transfers that take place in finite amounts of time can never recover all of the energy that was turned into entropy. This means the actual increase in entropy is always more than the amount that would occur in a reversible process:

$$
\Delta S = \frac{Q_{rev}}{T} \geq \frac{Q}{T}
$$

In other words, the energy that is lost to entropy by transfer of an amount of heat Q

would be exactly *Q T* for a completely reversible process (*i.e., Q* = *Qrev*), and more

than that for any real process.

Because actual heat transfer in a finite amount of time cannot be completely reversible, some heat is lost to the surroundings and the actual entropy change is always greater than the actual heat change at a given temperature. The concept of a reversible process is an idealization that represents the maximum amount of work that could theoretically be extracted from the process.

Consequences of the Second Law

- The total entropy of an isolated system can never decrease, and is constant only when all of the thermodynamic processes are reversible.
- Localized energy will tend to disperse (spread out). When this happens, thermal energy is lost to the surroundings, and the entropy of the system increases.
- Entropy is a state function, which means the entropy of a system does not depend on the energy pathway the system followed.
- Closed systems spontaneously move toward thermodynamic equilibrium (*i.e.,* all parts of the system have the same temperature). When a system has reached thermodynamic equilibrium, the system's entropy is maximized.
- Because the universe is a closed system, the entropy of the universe is always increasing.
- The entropy of an open system can be decreased through a transfer of energy into the system from the surroundings.

In physics, there is a hierarchy of thinking. Conservation of energy, conservation of momentum, and the Second Law are at the top of the hierarchy. Just as special relativity tells us that time, distance and mass all need to be changeable in order to maintain conservation of energy and momentum, the Second Law explains why time cannot move backwards—to do so would require a decrease in the entropy of the universe.

Third Law

The Third Law tells us that in an isolated system, the total energy of the system must be constant. (An isolated system is a system for which it is not possible to exchange energy with the surroundings.) This makes intuitive sense; because energy must be conserved, if no energy can be added or taken away, then the total energy cannot change.

Thermodynamic Quantities and Equations

Because energy is complex and exists in so many forms, there are many thermodynamic quantities that can be calculated in order to quantify the energy of different portions of a system. The following is a list of some of the more familiar ones:

Selected Thermodynamic Quantities

Because this is a physics course, we will leave enthalpy and Gibbs free energy to the chemists.

* Some chemistry textbooks use the variable *E* instead of *U*.

Thermodynamics Equations Used in This Course

Most of the thermodynamics problems encountered in this course are applications of the following equations:

What makes thermodynamics challenging is that there are many relationships between the quantities in these equations, as shown in the following thermodynamics equation map:

It is often necessary to combine equations. For example:

$$
\Delta U = \frac{3}{2} n R \Delta T = Q + W
$$

$$
-W = P \Delta V = n R \Delta T
$$

(Note that we moved the negative sign from $W = -P\Delta V$ to the other side of the equation.)

^{*} In an algebra-based course, we need to restrict ourselves to problems in which the pressure remains constant during volume changes. In a calculus-based course, this equation would be $W = -\int P dV$, where *P* is a function of *V*.

The problems that you will encounter will involve a change in a measurable state variable (pressure, volume and/or temperature). To solve these problems, you will need to:

- 1. Determine what the change involves:
	- heat transfer (*Q*)
	- work (W) resulting from a change in volume (ΔV) .
	- \bullet a change in internal energy (ΔU) resulting from a change in temperature (ΔT).

(There can be more than one of these happening at the same time.)

2. If necessary, determine initial and/or final values of these state variables in relation to other variables using equations such as:

•
$$
\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}
$$

- \bullet $PV = nRT$
- 3. Apply algebraic combinations of these equations to find each of the necessary quantities to answer the question.

Homework Problems

