Unit: Thermodynamics

Details

Big Ideas

MA Curriculum Frameworks (2016): HS-PS2-6

AP® Physics 2 Learning Objectives: 5.B.4.1, 5.B.5.4, 5.B.7.1, 7.B.2.1

Mastery Objective(s): (Students will be able to...)

• Calculate kinetic energy, internal energy and work done by the particles of a gas.

Success Criteria:

- Solutions have the correct quantities substituted for the correct variables.
- Algebra and rounding to appropriate number of significant figures is correct.

Language Objectives:

• Describe the different types of energy (kinetic, internal, work) and explain what they measure.

Tier 2 Vocabulary: internal, energy, work

Labs, Activities & Demonstrations:

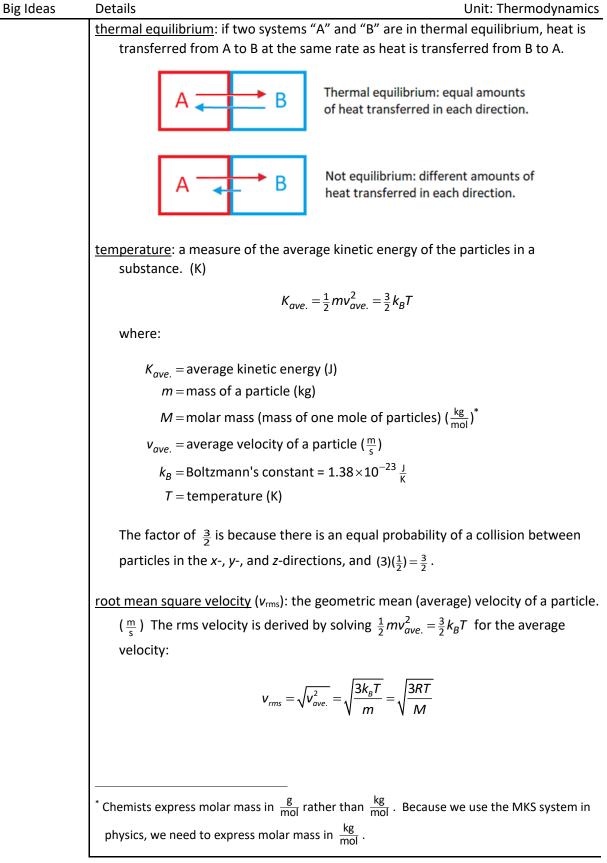
- heat exchange dice game
- dice distribution game
- entropy (microstates) percentile dice game

Notes:

thermodynamics: the study of heat-related (thermal) energy changes (dynamics)

Thermodynamics is an application of the law of conservation of energy. In Physics 1, we studied changes between gravitational potential energy and kinetic energy. Thermodynamic changes involve the same principle; the details and the equations, however, are quite different.

As was the case with gas laws, the topic of thermodynamics is studied by both chemists and physicists. Chemists tend to be more concerned with the heat produced and consumed by chemical changes and reactions. Physicists tend to be more concerned with the conversion between thermal energy (regardless of how it is produced) and other forms of energy, particularly mechanical.



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internal energy (U^*) : the total thermal energy of a system due to the kinetic energy of its particles.
If the kinetic energy of a single particle is $K_{ave.} = \frac{3}{2}k_BT$, then the total kinetic
energy in a system that has N particles would be:
$U = NK_{ave.} = \frac{3}{2}Nk_{B}T$
Because it is generally unwieldy to perform calculations for systems with large numbers of particles, it is more convenient to use moles. Substituting nR for Nk_B gives the equation for the internal energy of a system that has n moles of particles:
$U = \frac{3}{2} nRT$
Similarly, a <u>change</u> in internal energy (ΔU) is related to the corresponding <u>change</u> in temperature (ΔT):
$\Delta U = \frac{3}{2} nR \Delta T \ (= \frac{3}{2} N k_{B} \Delta T)$
heat (Q): thermal energy transferred into or out of a system. (J)
work (W): mechanical energy (such as the application of a force over a distance) transferred into or out of a system. (J)
The work that a gas can do comes from its ability to move an object by applying a force on it as it expands. If the pressure is constant:
$W = Fd = F\Delta x$
$P = \frac{F}{A} \longrightarrow F = PA$
$\therefore W = (PA)\Delta x$
$\Delta V = A \Delta x$
$\therefore W = P \Delta V$
If a gas does work by expanding, the energy is transferred from the gas (the system) to the object that the gas is pushing against (the surroundings). This means that when the volume increases (ΔV is positive), energy is leaving the system (W is negative). Conversely, if work is done to compress a gas, energy is entering the system in order to compress the gas (W is positive), and the volume decreases (ΔV is negative). This means that W and $P\Delta V$ must have opposite signs, which gives the equation:
$W = -P\Delta V$
assuming that pressure is constant.

* Chemistry textbooks often use the variable *E* instead of *U*.

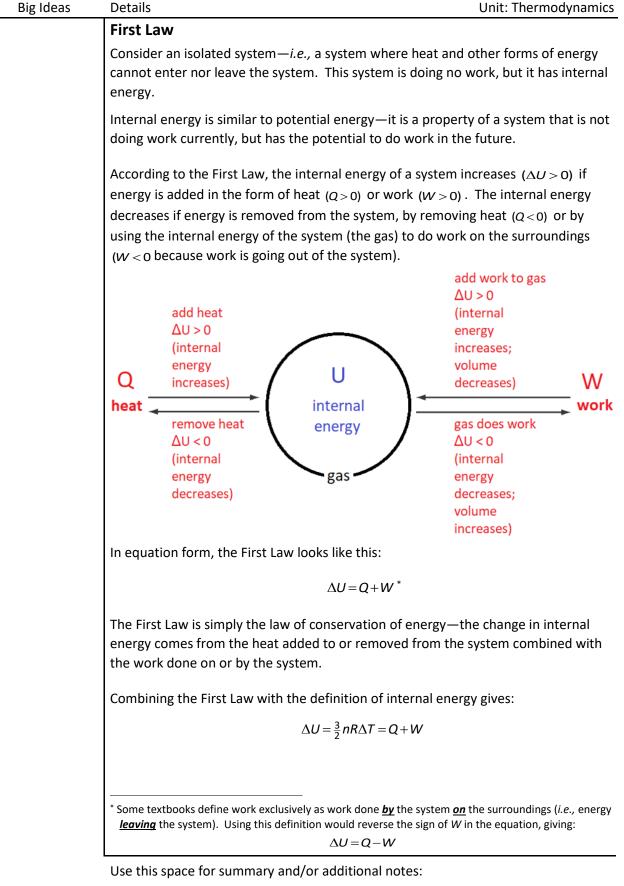
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Big Ideas

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Ideas	Details	Unit: Thermodynamic
	If pressure is not constant, then $W = -\Delta(PV)$, which r	means you would need to
	calculate PV at each point, taking the limit as the distant	
	points shrinks to zero, and add them up. In calculus,	this is the integral:
	$W = -\int P dV$, where <i>P</i> is a function of <i>V</i> .	
	In an algebra-based course, we will limit ourselves to pressure is constant, or where the pressure change is average pressure, giving:	•
	$W = -P_{ave.}\Delta V$	
	<u>entropy</u> (S): "unusable" thermal energy in a system. Ener unavailable because it has "escaped" or "spread out" further in the Second Law of Thermodynamics.)	
	Laws of Thermodynam	ics
	The laws of thermodynamics describe the behavior of sys	
		instand of 1. A base was the
	For historical reasons, the laws are numbered from 0−3 [*] i 0 law was added after the others, and the laws are often number.	
	 If a system is at thermal equilibrium, every composite same temperature. ("You have to play the game. 	•
	 Heat always flows from a region of higher internal lower internal energy. Because internal energy is temperature, this is equivalent to saying that hea higher temperature to a region of lower tempera get more heat out of a system than you put in. (" 	directly proportional to at flows from a region of ture. This means you can'
	 In almost every change, some energy is irretrieva surroundings. Entropy is a measure of this "lost" universe is always increasing, which means on an always get out less energy than you put in. ("You 	energy. The entropy of the practical scale, you will
	 Conservation of energy always applies. In any clo energy (internal energy + entropy + work) remain 	osed system, the total

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	Zeroth Law (or Zero Law)	
	The zeroth law says that if you have multiple systems in the heat transferred from "A" to "B" is equal to the heat transthen the systems must have the same temperature. The	sferred from "B" to "A"),
	 If we have three (or more) systems "A," "B," and "G equilibrium with B, and B is in thermal equilibrium B, and C must all have the same temperature, and equilibrium with C. (This is akin to the transitive pr mathematics.) 	with C, this means that A, A is therefore in thermal
	 If an object with a higher temperature (a "hotter" of object with a lower temperature (a "colder" object object with higher temperature to the object with temperatures are the same (the objects are in ther), heat will flow from the lower temperature until the

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	Sample Problem:	
	 Q: A cylinder containing 1.8 mol of an ideal gas with a temperature of 275 K has a piston with a weight on top. combined mass of the piston plus the weight is 2.0 kg, an the cross-sectional area of the piston is 0.01 m². The volu of the gas in the cylinder is 0.033 m³. 	id i i i i i i i i i i i i i i i i i i
	Heat is added, and the volume of the gas increases to 0.040 m ³ . How much heat was added to the gas?	
	A: When the gas is heated, the following occur:	
	1. In order to increase the volume, the gas has to expand which means the temperature needs to increase. We know how much the volume increased, and the press remains constant (the piston pushes the same amount throughout the presses). We can use $P_1V_1 = P_2V_2$ to fi	ure T t heat (Q)
	throughout the process). We can use $\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$ to fi	nu
	the final temperature of the gas.	
	$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2} \rightarrow \frac{0.033}{275} = \frac{0.040}{T_2} \rightarrow$	T ₂ = 333 K
	2. The increase in temperature means the internal energy We can use $\Delta U = \frac{3}{2}nR\Delta T$ to find out how much the in increased (ΔU). The equation $\Delta U = Q + W$ tells us that energy needed to be used for the increase in internal it was used to do the work of raising the piston.	ternal energy of the gas at some of the heat
	$\Delta U = \frac{3}{2} nR\Delta T \Rightarrow \Delta U = (\frac{3}{2})(1.8)(8.31)(333)$	-275)=1301 J
	3. We can calculate the work used to raise the piston from physics 1: $W = mg\Delta h$ (Note that $\Delta V = A\Delta h$.)	m the work equation
	$W = -mg\Delta h = -mg\frac{\Delta V}{A} = -(2)(10)\frac{0.007}{0.01} = -14$ J	
	The work is negative because the energy is going out of (remember that the system is the gas) and into the su	•
	4. Once we have ΔU and W , we can find Q by applying t	he first law:
	$\Delta U = Q + W$	
	1301 = Q + (-14)	
	1315 J=Q	
	Use this space for summary and/or additional notes:	

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	Alternatively, we could calculate the work using W	$Y = -P\Delta V$, but we would need
	to use gauge pressure rather than absolute pressur	e. (See the explanation
	below and gauge pressure on page 152.)	
	The first two steps are the same as above.	
	 This step is the same as step #1 above—we nee change necessary to produce the change in vol 	•
	 This step is the same as step #2 above—we nee internal energy of the gas caused by the change 	_
	3. Instead of calculating the work using equations $W = -P\Delta V$. However, pressure needs to be the doing the work, which is the difference in press the piston and the outside of the piston. (This inside the cylinder.) We can calculate this using the fluids unit (see Pressure, starting on page 1)	e amount of pressure that is sure between the inside of would be the gauge pressure g the pressure equation from
	$P = \frac{F}{A} = \frac{(2)(10)}{0.01} = 2000$	ОРа
	This is the pressure at which the gas needs to d	lo work.
	Once we have the pressure, the work is given b	by:
	$W = -P\Delta V$	
	$\Delta V = 0.040 - 0.033 = 0.007 \mathrm{m}^3$	
	W = -(2000)(0.007) = -14 J	
	4. Once we have ΔU and W , we can find Q by ap	plying the first law:
	$\Delta U = Q + W$	
	1301 = Q + (-14)	
	1315 J=Q	
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	Second Law	
	The Second law tells us that heat energy cannot flow from hotter one unless work is done on the system. This is why your ice cream melts.	•
	One consequence of this law is that no machine can work machines generate some heat, and some of that heat is al surroundings.	
	Entropy	
	Because energy must be conserved, we have to account for but has "gotten lost" ("escaped" or "spread out") and is no system. Energy that has spread out and cannot be recove	o longer usable by the
	For example, when an egg falls to the floor and breaks, gra energy is converted to a combination of internal energy (t the temperature of the egg), and entropy (heat energy tha environment and "lost"). Over time, the internal energy in to the environment and "lost" as the egg cools off. Ultima gravitational potential energy ends up converted to entrop energy that is dissipated and cannot be recovered.	he measurable increase in at is radiated to the n the egg is also radiated ately, all of the
	Entropy is sometimes called "disorder" or "randomness", sense this is not correct. The entropy of your room is a <i>th</i> the heat energy in your room, not a commentary on the a the floor!	ermodynamic property of
	Whenever heat is transferred from an object with a higher with a lower temperature, the heat "spreads out" as it wa amount of energy that goes into this "spread" is called ent	rms the colder object. The
	Q Heat Transfer T_1 (hot) $\Delta S = Entropy = \frac{Q}{T}$ Use this space for summary and/or additional notes:	T ₂ (cold)

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If the heat is transferred in a way that is completely reversible (which is impossible and would take an infinite amount of time), then you would be able to recover the energy that was converted to entropy when transferring it back to the hotter object. We call this fictitious heat "reversible heat," denoted Q_{rev} .

$$\Delta S = \frac{Q_{rev}}{T}$$

Real energy transfers that take place in finite amounts of time can never recover all of the energy that was turned into entropy. This means the actual increase in entropy is always more than the amount that would occur in a reversible process:

$$\Delta S = \frac{Q_{rev}}{T} \ge \frac{Q}{T}$$

In other words, the energy that is lost to entropy by transfer of an amount of heat Q

would be exactly $\frac{Q}{T}$ for a completely reversible process (*i.e.*, $Q = Q_{rev}$), and more

than that for any real process.

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Because actual heat transfer in a finite amount of time cannot be completely reversible, some heat is lost to the surroundings and the actual entropy change is always greater than the actual heat change at a given temperature. The concept of a reversible process is an idealization that represents the maximum amount of work that could theoretically be extracted from the process.

A consequence of the Second Law is that <u>the entropy of the universe is always</u> <u>increasing</u>.

In physics, there is a hierarchy of thinking. Conservation of energy, conservation of momentum, and the Second Law are at the top of the hierarchy. Just as special relativity tells us that time, distance and mass all need to be changeable in order to maintain conservation of energy and momentum, the Second Law explains why time cannot move backwards—to do so would require a decrease in the entropy of the universe.

Third Law

The Third Law tells us that in an isolated system, the total energy of the system must be constant. (An isolated system is a system for which it is not possible to exchange energy with the surroundings.) This makes intuitive sense; because energy must be conserved, if no energy can be added or taken away, then the total energy cannot change.

Thermodynamic Quantities and Equations

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Because energy is complex and exists in so many forms, there are many thermodynamic quantities that can be calculated in order to quantify the energy of different portions of a system. The following is a list of some of the more familiar ones:

Variable	Name	Description
Q	heat	Thermal energy (heat) transferred into or out of a system due to a difference in temperature.
W	work	Mechanical energy transferred into or out of a system through the action of a force applied over a distance. $W = \vec{F} \cdot \vec{d} = -P \Delta V$
U*	internal energy	Total thermal (non-chemical) energy contained within the particles of a system because of their kinetic energy. $U = \frac{3}{2}nRT \qquad \Delta U = Q + W = \frac{3}{2}nR\Delta T$
S	entropy	Energy that is "lost" (inaccessible) because it has spread to the surroundings or has spread to separate microstates and cannot be utilized by the particles of the system.
A	Helmholtz free energy	Useful work that could theoretically be obtained from a system. $A = U - TS \qquad \Delta A = \Delta U - T\Delta S$
Н	enthalpy	Heat energy available in a chemical reaction. $H = U + PV$ $\Delta H = \Delta U + P\Delta V = \Delta U - W$
G Gibbs free energy		Total energy available in a chemical reaction. $G = H - TS$ $\Delta G = \Delta H - T\Delta S$

Selected Thermodynamic Quantities

Because this is a physics course, we will leave enthalpy and Gibbs free energy to the chemists.

* Some chemistry textbooks use the variable *E* instead of *U*.

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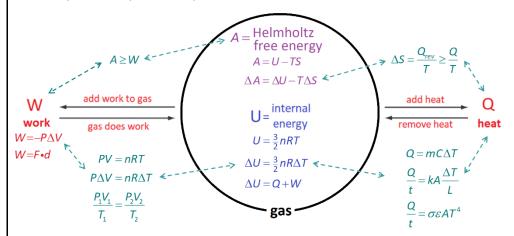
Big Ideas



Most of the thermodynamics problems encountered in this course are applications of the following equations:

Equation	Quantities that are Changing	
$U=\frac{3}{2}nRT$		
$\Delta U = \frac{3}{2} nR\Delta T$	internal energy vs. temperature	
$\Delta U = Q + W$	internal energy vs. heat & work	
PV = nRT	pressure & volume vs. temperature	
$P\Delta V = nR\Delta T$		
$W = -P\Delta V^*$	work <i>vs.</i> volume	

What makes thermodynamics challenging is that there are many relationships between the quantities in these equations, as shown in the following thermodynamics equation map:



It is often necessary to combine equations. For example:

$$\Delta U = \frac{3}{2} nR\Delta T = Q + W$$
$$-W = P\Delta V = nR\Delta T$$

(Note that we moved the negative sign from $W = -P\Delta V$ to the other side of the equation.)

* In an algebra-based course, we need to restrict ourselves to problems in which the pressure remains constant during volume changes. In a calculus-based course, this equation would be $W = -\int P dV$.

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 The problems that you will encounter will involve a change in a measurable state

 variable (pressure, volume and/or temperature). To solve these problems, you will

 need to:

- 1. Determine what the change involves:
 - heat transfer (Q)

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- work (*W*) resulting from a change in volume (ΔV).
- a change in internal energy (ΔU) resulting from a change in temperature (ΔT).

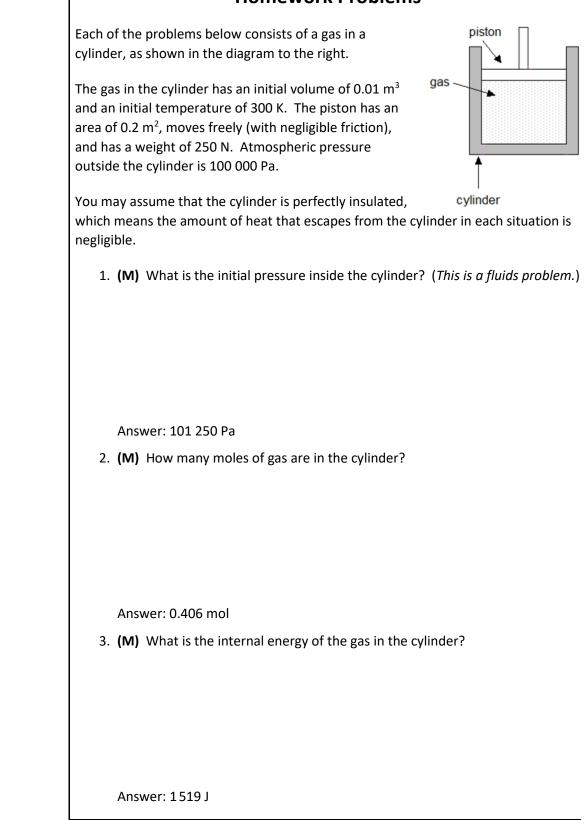
(There can be more than one of these happening at the same time.)

2. If necessary, determine initial and/or final values of these state variables in relation to other variables using equations such as:

•
$$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$$

- PV = nRT
- 3. Apply algebraic combinations of these equations to find each of the necessary quantities to answer the question.

Homework Problems

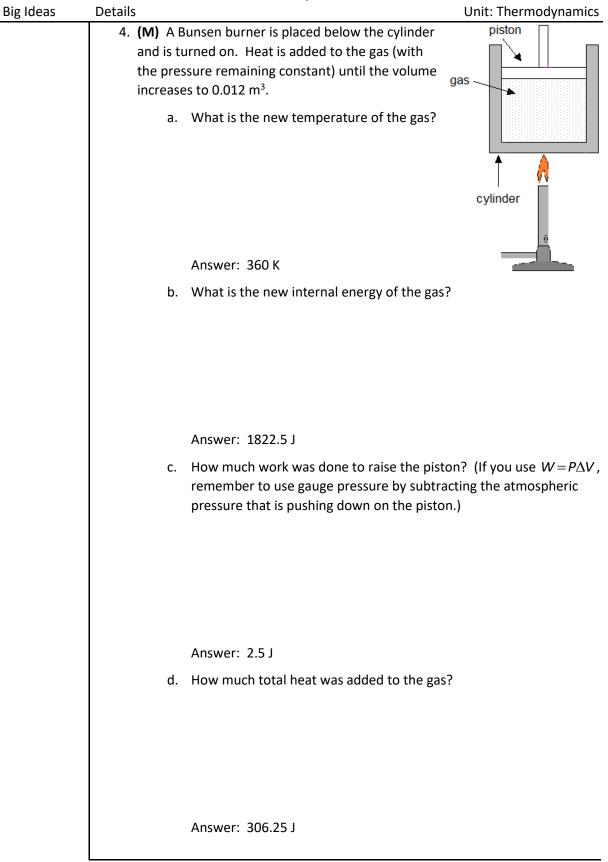


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	5.	(M) Sup	pose instead that the piston from problem #4 above was fixed in
		position	and was not allowed to move, so the volume remains constant at
		0.01 m ³	while the 306.25 J of heat from question 4d was added.
		a.	What is the new temperature of the gas?
			Answer: 360.5 K
		b.	What is the new pressure of the gas?
			Answer: 121 667 Pa
		С.	If the piston is then released and allowed to move freely, what will the new pressure be inside the cylinder?
			the new pressure be inside the cylinder!
			Answer: 101 250 Pa (the same as in problem #1 above)

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